

# Geometry Lesson 56

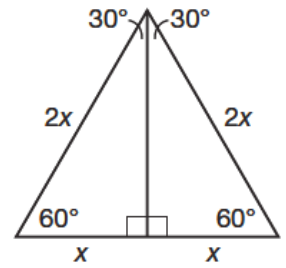
Objective: TSW use  $30^\circ - 60^\circ - 90^\circ$  right triangles.

Date: \_\_\_\_\_

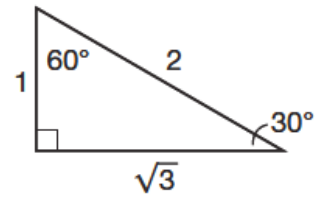
Period: \_\_\_\_\_

The  $30^\circ-60^\circ-90^\circ$  triangle is another special triangle. Like the  $45^\circ-45^\circ-90^\circ$  triangle, properties of the  $30^\circ-60^\circ-90^\circ$  triangle can be used to find missing measures of a triangle if the length of one side is known.

In the diagram, two  $30^\circ-60^\circ-90^\circ$  triangles are shown next to each other, with the shorter legs aligned. Placing the two triangles together so that they share a common leg makes an equilateral triangle. Since all the equilateral triangle's sides are congruent, this shows that the hypotenuse of the triangle is twice the length of the shortest leg.

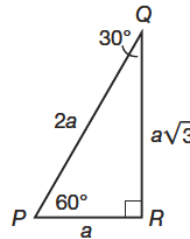


Properties of  $30^\circ-60^\circ-90^\circ$  Triangles - In a  $30^\circ-60^\circ-90^\circ$  triangle, the length of the hypotenuse is twice the length of the short leg, and the length of the longer leg is the length of the shorter leg times \_\_\_\_\_.



Algebraically, these relationships can be written as follows.

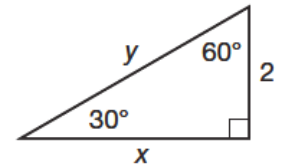
$$PR = \underline{\hspace{1cm}} \quad PQ = \underline{\hspace{1cm}} \quad QR = \underline{\hspace{1cm}}$$



Example 1 Finding Side Lengths in a  $30^\circ-60^\circ-90^\circ$  Triangle

Find the values of  $x$  and  $y$ . Give your answer in simplified radical form.

SOLUTION

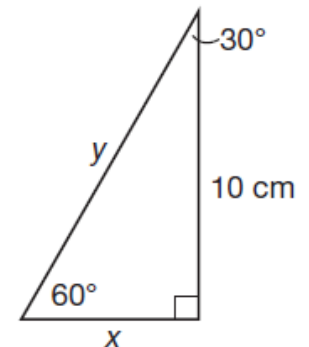


Example 2 Finding the Perimeter of a  $30^\circ-60^\circ-90^\circ$  Triangle with Unknown Measures

Find the perimeter of the triangle. Give your answer in simplified radical form.

SOLUTION

First, find the length of  $x$  and  $y$ . The short leg is  $x$ . Since the length of the short leg times the square root of 3 equals the long leg, an equation can be written to solve for  $x$ .



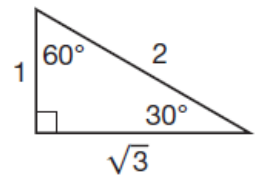
## Caution

As in Lesson 53, be sure to rationalize any fraction with a square root in the denominator by multiplying both the numerator and denominator by that root.

Since the length of the short leg is now known, the length of the hypotenuse can be found by multiplying the short leg by 2.

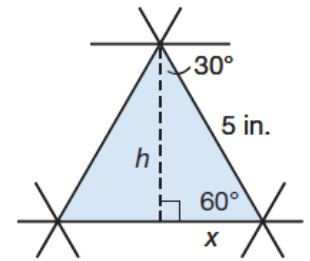
Now that the lengths of all the sides are known, calculate the perimeter.

Instead of memorizing the algebraic expressions for each side of a  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle, it may be helpful to just remember the triangle in the diagram, with side lengths 1,  $\sqrt{3}$ , and 2.



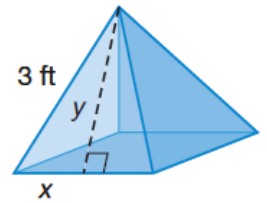
**Example 3 Applying the Pythagorean Theorem with  $30^\circ$ - $60^\circ$ - $90^\circ$  Right Triangles**  
 Each tile in a pattern is an equilateral triangle. Find the area of the tile. Use the Pythagorean Theorem and give your answer in simplified radical form.

**SOLUTION**



Example 4 Application: Engineering

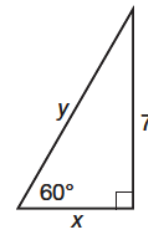
A museum exhibit contains a model of a pyramid. It has equilateral triangles for faces, and each side of a face is 3 feet long. For a restoration project, the exhibit designers need to know the area of one face of the pyramid. Find this area.



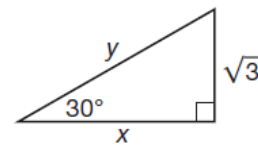
SOLUTION

You Try!!!!

a. Find the length of each side of the triangle.



b. Find the perimeter of the triangle in simplified radical form.



c. A school's banner is an equilateral triangle shown here.

Use the Pythagorean Theorem to find the area of the equilateral triangle.



d. Find the area of one triangular face of a pyramid. The faces of the pyramid are equilateral triangles with sides that are 12 centimeter each.