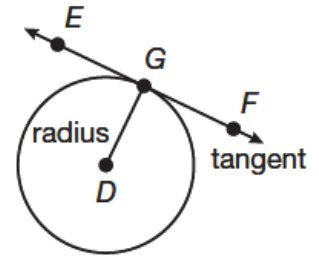


Geometry Lesson 58

Objective: TSW use tangents and circles (Part 1).

A tangent line lies in the same plane as a circle and intersects the circle at exactly one point. A radius of a circle drawn to a point of tangency meets the tangent line at a fixed angle.

Theorem 58-1 - If a line is tangent to a circle, then the line is perpendicular to a radius drawn to the point of tangency.



Example 1 Tangent Lines and Angle Measures

Line n is tangent to $\odot C$ at point P , and line m passes through C .

Lines n and m intersect at point Q .

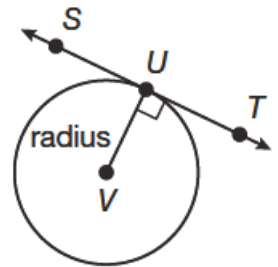
a. Sketch $\odot C$ and lines n and m . Mark C , P , and Q on your sketch.

SOLUTION

b. If $m\angle CQP = 36^\circ$, determine $m\angle PCQ$.

SOLUTION

Theorem 58-2 - If a line in the plane of a circle is perpendicular to a radius at its endpoint on the circle, then the line is tangent to the circle.



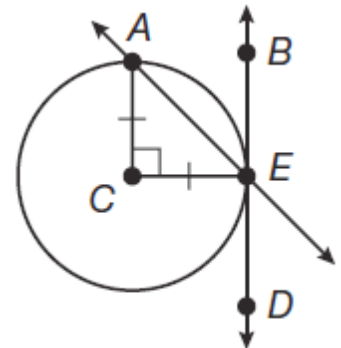
Theorem 58-2 is the converse of Theorem 58-1. Together, they can be used to show that this biconditional statement is true:

A line in the plane of a circle is tangent to the circle if and only if it is perpendicular to a radius drawn to the point of tangency.

Example 2 Identifying Tangent Lines

If $m\angle BEA = 45^\circ$, show that \overleftrightarrow{BD} is tangent to $\odot C$.

SOLUTION



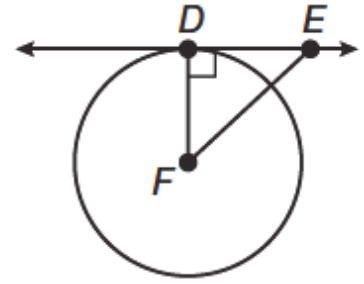
Example 3 Proving Theorem 58-2

Prove Theorem 58-2.

Given: $\overleftrightarrow{DE} \perp \overline{FD}$ and D is on \odot .

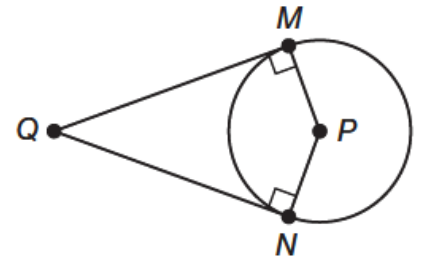
Prove: \overleftrightarrow{DE} is tangent to \odot .

SOLUTION



If two tangents to the same circle intersect, the tangent segments exhibit a special property, stated in Theorem 58-3.

Theorem 58-3 - If two tangent segments are drawn to a circle from the same exterior point, then they are congruent.

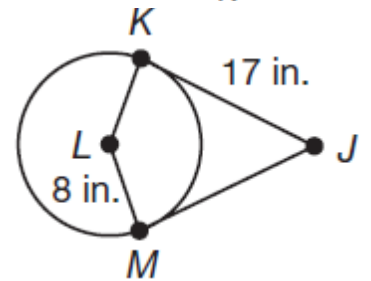


Example 4 Applying Relationships of Tangents from an Exterior Point

In this figure, \overline{JK} and \overline{JM} are tangent to $\odot L$.

Determine the perimeter of quadrilateral $JKLM$. What type of quadrilateral is $JKLM$?

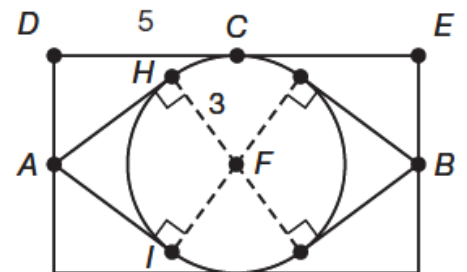
SOLUTION



Example 5 Application: Glass Cutting

An ornamental window has several glass panes oriented to look like an eye. The radius of the eye's iris is 3 feet, and DC is 5 feet. What are AI and AH ?

SOLUTION



You Try!!!!

a. Line a is tangent to $\odot R$ at D , and line b passes through R . Lines a and b intersect at E . If $m\angle RED = 42^\circ$, determine $m\angle DRE$.

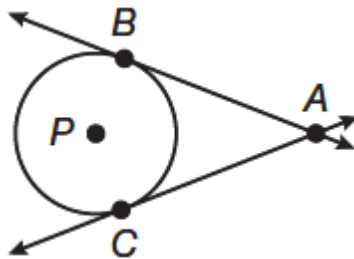
b. Let \overline{CA} be a radius of $\odot C$. Let line m be tangent to $\odot C$ at A . Let B be an exterior point of $\odot C$, with $m\angle BAC < 90^\circ$. Is \overline{AB} a tangent to $\odot C$? Why or why not?

c. Give a paragraph proof of Theorem 58-3.

Hint: Draw \overline{PA} , \overline{PB} , and \overline{PC} .

Given: \overline{AB} and \overline{AC} are tangent to $\odot P$

Prove: $\overline{AB} \cong \overline{AC}$



d. Circle C has a 5-inch radius. \overline{XZ} and \overline{YZ} are tangents to $\odot C$ and Z is exterior to $\odot C$.

If $\angle XCY$ is a right angle, what is the area of quadrilateral $CXZY$?

e. A decorative window is shaped like a triangle with an inscribed circle. If the triangle is an equilateral triangle, the circle has a radius of 3 feet, and CQ is 6 feet, what is the perimeter of the triangle in simplified radical form?

