Geometry Lesson 75

Objective: TSW write the equation of a circle.

Date: _____

Name:

Period: _____

To analyze a circle on a coordinate plane, it is necessary to derive an equation for the graph of a circle. A simple version of this equation can be found by looking at circles that are centered at the origin.

Example 1 Analyzing a Circle Centered at the OriginSuppose P(x, y) is a point on the circle with a 1-unit radius that is centered at the origin.What is QP ? How is QP related to x and y?SOLUTION



The **unit circle** is a circle with a radius of 1, centered at the origin. The unit circle is frequently used in trigonometry.



The equation given above, $x^2 + y^2 = 1$, gives a relationship between x and y that is true of all points that lie on the circle. Therefore, it is an equation for the circle with a radius of 1 that is centered at the origin. Any circle centered at the origin has an equation given by $x^2 + y^2 = r$, where r is the radius.



If the circle is not centered at the origin, this alters the equation. Examine the circle centered at (2, 0) with a radius of 2. For the point (*x*, *y*), the distance from the center of the circle to (*x*, *y*) is $\sqrt{(x-2)^2 + (y-0)^2} = 2$, by the distance formula. So the equation for this circle is $(x-2)^2 + y^2 = 4$.

The Equation of a Circle - The equation of a circle is given by the following formula, where (h, k) is the center of the circle and r is the radius of the circle.

Example 2 Writing the Equation for a Circle from a Graph a. If A is a point on $\bigcirc D$, write the equation of $\bigcirc D$. SOLUTION



Math Language

Two circles are concentric if they have the same center.

b. Circle *E* is concentric with $\bigcirc D$ and has a radius of 5. Write the equation of $\bigcirc E$. SOLUTION

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Example 3 Graphing a Circle Given its Equation

a. The equation of $\bigcirc P$ is $x^2 + y^2 = 25$. Graph $\bigcirc P$. SOLUTION



b. The equation of $\bigcirc Q$ is $(x - 2)^2 + (y + 1)^2 = 16$. Graph $\bigcirc Q$. SOLUTION



Example 4 Application: Astronomy

This coordinate grid shows a satellite's orbit around Earth, which is located at the origin. If the satellite's distance from Earth is 23,000 miles, write an equation that describes the satellite's circular orbit.

SOLUTION



You Try!!!!

a. If M(x, y) is a point on a circle centered at the origin with a radius of 3, what is *PM*, and what is the equation of the circle?

b. Write an equation to relate all the *x*- and *y*-coordinates of points that lie on $\bigcirc A$

with a radius of $\sqrt{2}$, which is centered at the origin.

c. Write the equation for $\bigcirc B$.



d. Circle *C* is concentric with $\bigcirc B$ and has a radius of 3.5. Write the equation of $\bigcirc C$.

e. The equation of $\bigcirc D$ is $x^2 + y^2 = 6.25$. Graph $\bigcirc D$.

f. The equation of $\bigcirc E$ is $(x + 1)^2 + (y - 3)^2 = 4$. Graph $\bigcirc E$.

g. Sports: This coordinate grid shows the position of the lines on a basketball court. The center circle crosses the half court line at A(47, 19) and B(47, 31), so \overline{AB} is a diameter. What is

the equation of the center circle?



